



Climate stability of habitable Earth-like planets



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ABSTRACT

The carbon–silicate cycle regulates the atmospheric CO₂ content of terrestrial planets on geological timescales through a balance between the rates of CO₂ volcanic outgassing and planetary intake from rock weathering. It is thought to act as an efficient climatic thermostat on Earth and, by extension, on other habitable planets. If, however, the weathering rate increases with the atmospheric CO₂ content, as expected on planets lacking land vascular plants, the carbon–silicate cycle feedback can become severely limited. Here we show that Earth-like planets receiving less sunlight than current Earth may no longer possess a stable warm climate but instead repeatedly cycle between unstable glaciated and deglaciated climatic states. This has implications for the search for life on exoplanets in the habitable zone of nearby stars.

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1. Introduction

It is generally thought that the carbon–silicate cycle acts as a stabilizing feedback and a powerful thermostat for the Earth climate, guaranteeing surface liquid water conditions. Above freezing temperatures, rock weathering occurs faster at higher temperatures, which reduces the CO₂ atmospheric partial pressure, $p\text{CO}_2$, and cools down the climate. Conversely, on a frozen planet that temporarily lacks weathering, atmospheric CO₂ builds up from continued volcanic outgassing, which warms up the climate until surface liquid water and weathering conditions are restored (Walker et al., 1981; Kasting et al., 1993; Kump et al., 2000). Such $p\text{CO}_2$ build up is in fact the leading scenario for the deglaciation of Earth following a snowball event (Kirschvink, 1981; Hoffman et al., 1998; Hoffman and Schragg, 2002). Generalizations of these concepts to Earth-like planets around other stars are central to the definition of their liquid water habitable zone (Kasting et al., 1993; Forget and Pierrehumbert, 1997; Kopparapu et al., 2013). In particular, planets subject to modest levels of insolation are expected to achieve temperate conditions with liquid water at the surface by building up massive enough CO₂ atmospheres (Kasting et al., 1993; Williams and Kasting, 1997; Selsis et al., 2007).

Experimental data, theoretical arguments and paleoclimate modeling suggest that the rate of CO₂ intake via rock weathering

by a planet lacking land vascular plants increases with the atmospheric CO₂ content, $p\text{CO}_2$ (Walker et al., 1981; Kump et al., 2000; Schwartzman and Volk, 1989; Berner, 1992, 1994; Berner and Kothavala, 2001). This feature of lifeless planets or planets with only primitive forms of life is important because it will limit the buildup of CO₂ at high values. As a result, the climate thermostat due to the carbon–silicate cycle should become less efficient on weakly-insolated Earth-like planets located in the outer regions of the habitable zone.

2. Climate-weathering models

To address this issue quantitatively, we model Earth-like climates on planets around Sun-like stars with a zero-dimensional, energy balance model that equates the net insolation and thermal radiation fluxes,

$$\frac{S}{4} [1 - \alpha(T_{\text{surf}}, p\text{CO}_2)] = \text{OLR}(T_{\text{surf}}, p\text{CO}_2), \quad (1)$$

where S is the insolation flux, α is the planetary Bond albedo and OLR is the outgoing longwave radiation flux emitted by the planet. OLR and α are functions of the surface temperature, T_{surf} , and $p\text{CO}_2$, derived from radiative–convective climate models (Williams and Kasting, 1997) (see Appendix A for details).

While we assume that the climate reaches thermal equilibrium rapidly, by virtue of Equation (1), the slower CO₂ compositional equilibrium is not imposed a priori in our models. Rather, $p\text{CO}_2$ is evolved on the relevant geological timescales according to

$$\frac{d}{dt} p\text{CO}_2 = V - W(T_{\text{surf}}, p\text{CO}_2), \quad (2)$$

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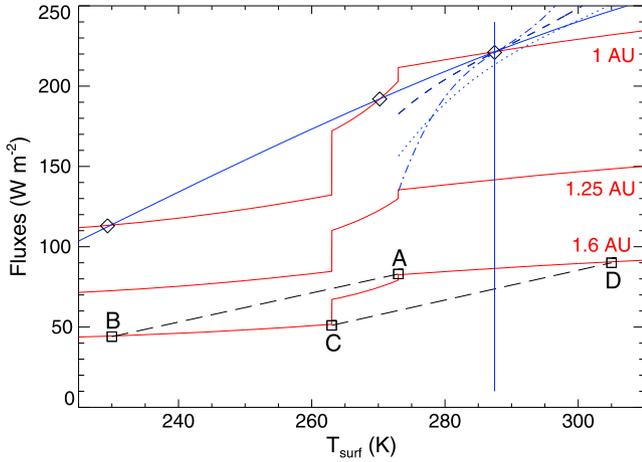


Fig. 1. Climate at global radiative equilibrium for an Earth-like planet. Red lines show the albedo-corrected insolation (heating) flux as a function of surface temperature, T_{surf} , at 1 AU (top), 1.25 AU (middle) and 1.6 AU (bottom) from a Sun-like star. Blue lines show the infrared cooling flux (OLR) according to various scenarios for the atmospheric CO_2 content (slanted solid line: fixed $p\text{CO}_2$ model; dashed: $\beta = 0.5$ weathering model; dotted: $\beta = 0.5$ weathering model with 3 times larger CO_2 outgassing rate; dash-dotted: $\beta = 0.25$ weathering model; vertical solid: $\beta = 0$ weathering model). When no stable climate exists at large orbital distances (absent blue–red intersections), the climate must repeatedly cycle through points A–B–C–D shown in the 1.6 AU case, with a slow $p\text{CO}_2$ build-up (B–C), a transition to a hot climate (C–D), a weathering period with decreasing $p\text{CO}_2$ (D–A) and a transition to global glaciation (A–B). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

where V is the global CO_2 volcanic outgassing rate (estimated as $V_{\oplus} = 7$ bars/Gyr for Earth, Abe et al., 2011) and W is the rate of CO_2 intake by the solid planet via rock weathering. The functional form of W is adapted from Earth studies for pre-vascular plant conditions (Bernier and Kothavala, 2001):

$$\frac{W}{W_{\oplus}} = \left(\frac{p\text{CO}_2}{p_{\oplus}} \right)^{\beta} e^{[k_{\text{act}}(T_{\text{surf}} - 288)]} \times [1 + k_{\text{run}}(T_{\text{surf}} - 288)]^{0.65}, \quad (3)$$

where $p_{\oplus} = 330 \mu\text{bar}$ is the pre-industrial $p\text{CO}_2$ level, $W = W_{\oplus} \equiv V_{\oplus}$ for $T_{\text{surf}} = 288$ K, $k_{\text{act}} = 0.09$ is related to an activation energy and $k_{\text{run}} = 0.045$ is a runoff efficiency factor. Varying Bernier and Kothavala (2001) k_{act} in the 0.06–0.135 range and k_{run} in the 0.025–0.045 range has only a minor quantitative impact on our results. Values of $\beta = 0.25$ –1 have been considered in the literature (Kump et al., 2000; Bernier, 1992; Abbot et al., 2012; Pierrehumbert, 2010) for the dependence of weathering on $p\text{CO}_2$ in the absence of land vascular plants. We use $\beta = 0.5$ (default) and 0.25 in this work. Note that equations (1) and (2) are coupled through $p\text{CO}_2$ and T_{surf} .

3. Climate solutions

3.1. Steady-state solutions

Steady-state climate solutions, satisfying both radiative (Equation (1)) and weathering equilibrium ($d/dt \equiv 0$ in Equation (2)) are represented in Fig. 1 by intersecting cooling and heating curves. Solid red lines in Fig. 1 show the albedo-corrected insolation flux (LHS of Equation (1)) received by a planet located at 1, 1.25 and 1.6 AU from a Sun-like star as a function of surface temperature.¹

Net insolation drops precipitously from 273 K to 263 K as the planetary surface freezes and the albedo reaches ~ 0.65 . The various blue lines in Fig. 1 represent the OLR cooling flux (RHS of Equation (1)) according to various scenarios for the atmospheric CO_2 content.

A standard model with $p\text{CO}_2$ arbitrarily fixed at $p_{\oplus} = 330 \mu\text{bar}$ (i.e. not constrained by Equation (2)) is represented by the slanted solid blue line. As is well known (Budyko, 1969; Sellers, 1969; North et al., 1981), three steady-state climate solutions exist in such a model for an Earth-like planet at 1 AU, as indicated by diamonds where the red and blue curves intersect. Earth's current climate ($T_{\text{surf}} \simeq 288$ K) and a globally-frozen state ($T_{\text{surf}} \simeq 229$ K) are both stable, while the intermediate state ($T_{\text{surf}} \simeq 270$ K) is thermally unstable.

However, when $p\text{CO}_2$ is also required to satisfy weathering equilibrium (Equation (2)), steady-state climate + weathering solutions only exist above freezing temperatures since weathering stops operating on a frozen planet. A model including weathering without any $p\text{CO}_2$ dependence ($\beta = 0$ in Equation (3)) is represented by the vertical solid blue line in Fig. 1. In such a model, weathering equilibrium enforces a unique surface temperature, set by requiring that weathering balances volcanic outgassing in Equation (2), and $p\text{CO}_2$ is only indirectly constrained by the constant T_{surf} requirement.

On the other hand, when the weathering rate depends on both $p\text{CO}_2$ and T_{surf} , noticeable bends appear in the blue cooling curves shown in Fig. 1. Indeed, in this class of models, the reduced efficiency of weathering at low temperatures must be balanced by large $p\text{CO}_2$ values to match the volcanic outgassing rate V . The weaker the weathering $p\text{CO}_2$ dependence, the stronger is the $p\text{CO}_2$ build-up at low surface temperatures (compare $\beta = 0.5$ and 0.25 models represented by the dashed and dash-dotted lines in Fig. 1, respectively). A planet with a larger volcanic CO_2 outgassing rate (Kite et al., 2009) achieves a warmer stable climate ($T_{\text{surf}} \simeq 292$ K for $V = 3V_{\oplus}$ and adopting our default weathering parameters, which is the case shown as a dotted line in Fig. 1).

Interestingly, stable climate + weathering solutions can cease to exist at low insolation levels, such as the 1.25 and 1.6 AU cases shown in Fig. 1, for a strong enough dependence of the weathering rate on $p\text{CO}_2$. For example, we find that blue curves no longer intersect with heating (insolation) lines beyond 1.077 AU if $\beta = 0.5$ and beyond 1.25 AU if $\beta = 0.25$. Conversely, a very weak weathering dependence on $p\text{CO}_2$ ($\beta < 0.1$), including the singular case $\beta = 0$ (vertical solid blue line in Fig. 1), do permit stable climate + weathering solutions at almost arbitrarily low insolation levels (Williams and Kasting, 1997). Low β values may be the relevant limit for planets where land vascular plants are widespread (Kump et al., 2000; Schwartzman and Volk, 1989; Bernier, 1992, 1994; Bernier and Kothavala, 2001; Pierrehumbert, 2010). On the other hand, for values of $\beta \sim 0.25$ –0.5 appropriate for planets lacking land vascular plants (Kump et al., 2000; Schwartzman and Volk, 1989; Bernier, 1992, 1994; Bernier and Kothavala, 2001; Pierrehumbert, 2010), the bending of cooling curves seen in Fig. 1 also implies that at fixed volcanism rate, V , less insolated planets achieve climate + weathering equilibrium at gradually lower T_{surf} values. For example, in the case $\beta = 0.25$, equilibrium is only marginally achieved above freezing temperatures at 1.25 AU, as shown in Fig. 1. At low enough insolation levels (far enough away from the star), climate + weathering equilibrium is no longer possible above freezing temperatures, which implies that weathering equilibrium is unattainable.

¹ Even though the planetary albedo α in Equation (1) depends on $p\text{CO}_2$, we find that this dependence is quantitatively negligible for $p\text{CO}_2 \ll 0.2$ bar. For simplicity, we plot heating (red) curves in this low $p\text{CO}_2$ limit in Fig. 1, which is indeed sat-

isfied by all the cooling (blue) curves shown. All our other results fully account for the α - $p\text{CO}_2$ dependence.

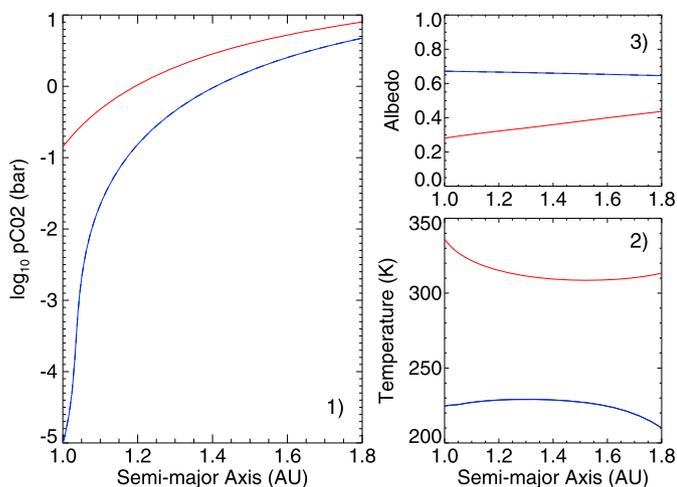


Fig. 2. Values of atmospheric partial CO_2 pressure (1), surface temperature (2) and planetary albedo (3) at extremes of the climate cycle illustrated in Fig. 1, as a function of orbital distance from a Sun-like star. Blue curves correspond to point B (cold, high albedo, low $p\text{CO}_2$) and red curves to point D (hot, low albedo, high $p\text{CO}_2$) of the cycle shown in Fig. 1. (For interpretation of the references to color in this figure, the reader is referred to the web version of this article.)

On planets lacking weathering equilibrium, the climate must repeatedly cycle through a succession of radiative equilibria as illustrated in Fig. 1: rapid transition from marginal to full glaciation (A \rightarrow B, at fixed $p\text{CO}_2$), slow build-up of $p\text{CO}_2$ caused by volcanic outgassing in the absence of weathering (B \rightarrow C), rapid transition to a deglaciated state (C \rightarrow D, at fixed $p\text{CO}_2$) and gradual $p\text{CO}_2$ decay under the action of weathering (D \rightarrow A), until the cycle repeats again with full glaciation. The general properties of the four critical points A–B–C–D of this climate cycle, which are independent of details of the weathering model, are quantified in Fig. 2 as a function of details of the weathering model, are quantified in Fig. 2 as a function of orbital distance from a Sun-like star. Blue curves correspond to the coldest cycle point with the lowest $p\text{CO}_2$ value, B, while the red curves correspond to the hottest point with the highest $p\text{CO}_2$ value, D.

Fig. 2 shows that Earth-like planets at larger orbital distances glaciates and deglaciates at larger $p\text{CO}_2$ values. A deglaciation with $p\text{CO}_2 \simeq 0.14$ bar at 1 AU is consistent with values reported for snowball Earth deglaciation (Hoffman and Schragg, 2002). Planets beyond 1.3 AU support massive (>0.3 bar) CO_2 atmospheres throughout their climate cycle. Planets in the frozen state have albedos $\simeq 0.65$, while the albedo of unfrozen planets rises from $\simeq 0.3$ to 0.45 in the 1–1.8 AU range, from an increasing atmospheric scattering contribution. The extremes of surface temperature along the cycle vary modestly with insolation level, with $T_{\text{surf}} \simeq 210$ –225 K at the coldest point and 310–330 K at the hottest point.

3.2. Climate cycles

Explicit time-dependent integrations of the system of Equations (1)–(3) reveal details of the climate cycle illustrated in Fig. 1. We initiated these integrations at the hot, high $p\text{CO}_2$ (weathering-independent) point D and confirmed that Earth-like planets receiving sufficiently large insolation fluxes settle to a steady-state warm climate solution after relaxation to weathering equilibrium. By contrast, planets at large enough orbital distances (low enough insolation levels) experience large amplitude climate cycles, as anticipated from our discussion of equilibrium solutions in relation to Fig. 1.

Fig. 3 shows six illustrative examples (A–F) of such climate cycles, shown in terms of variable T_{surf} and $p\text{CO}_2$ curves. Most of the cycle time is spent in the frozen state, during which $p\text{CO}_2$ build-up

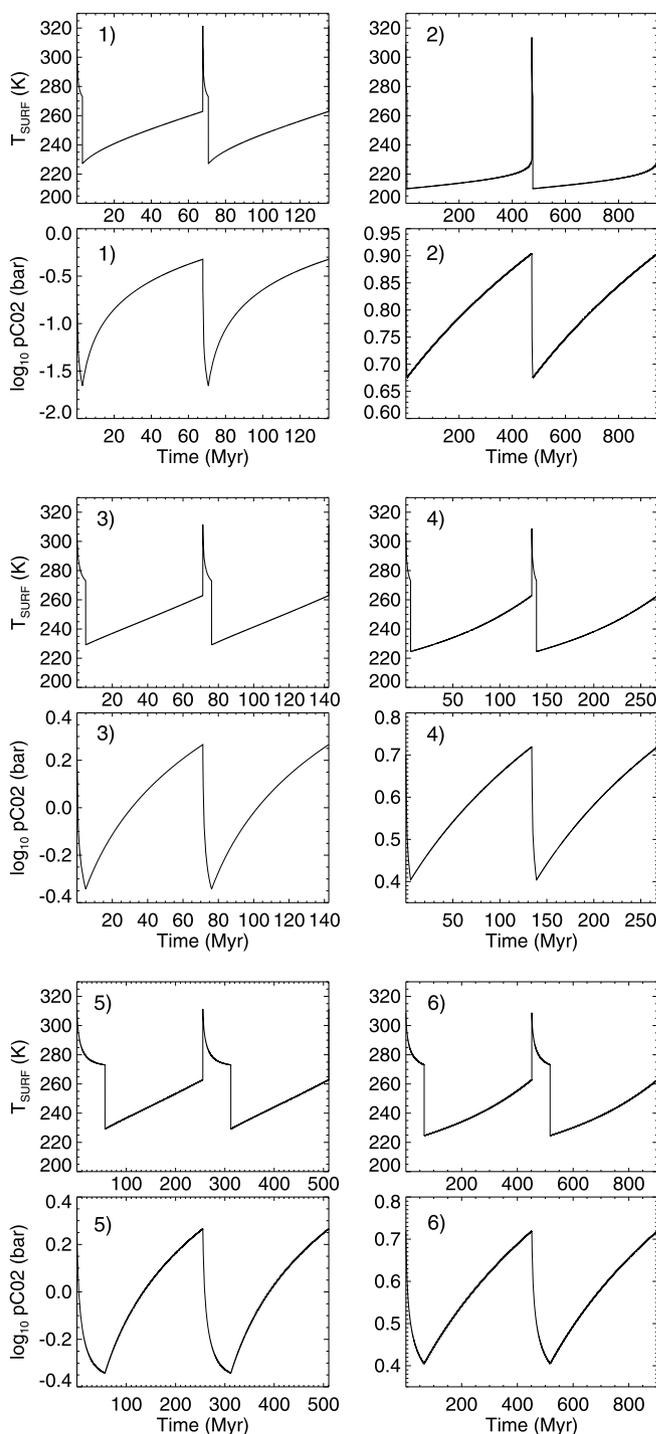


Fig. 3. Six examples of time-evolved climate cycles, with two full cycles shown in each case. For each model (1–6), the evolution of atmospheric partial CO_2 pressure (lower panel) and surface temperature (upper panel) are shown. Model 1: Default weathering model at 1.1 AU ($\beta = 0.5$ in Equation (3)). Model 2: Default weathering model at 1.8 AU. Model 3: 3 times larger CO_2 outgassing rate at 1.3 AU. Model 4: 3 times larger CO_2 outgassing rate at 1.6 AU. Model 5: Weaker $p\text{CO}_2$ weathering dependence ($\beta = 0.25$) at 1.3 AU. Model 6: Weaker $p\text{CO}_2$ weathering dependence ($\beta = 0.25$) at 1.6 AU. Increasing the CO_2 outgassing rate shortens the duration of the cold, CO_2 build-up phase. Weakening the weathering $p\text{CO}_2$ dependence ($\beta = 0.25$ rather than 0.5) lengthens the duration of the hot weathering phase, resulting in a much larger fraction of time spent with surface liquid water.

is slow compared to the fast weathering that occurs at above-freezing temperatures. In model 1, 4.6% of the 70 Myr cycle is spent in a warm state with surface liquid water. The corresponding numbers are 0.8% of 477 Myr in model 2, 7.5% of 76 Myr in model

3, 3.9% of 139 Myr in model 4, 28% of 312 Myr in model 5 and 17% of 517 Myr in model 6. Faster weathering at higher T_{surf} also implies that most of the time in the unfrozen state is spent just above freezing temperatures, near the lowest $p\text{CO}_2$ levels covered during the cycle. For a fixed volcanic outgassing rate, V , the climate cycle duration increases with decreasing insolation because larger absolute $p\text{CO}_2$ values must be reached for climate transitions to occur (Fig. 2). Decreasing insolation also reduces the fraction of cycle time spent with surface liquid water by the planet, although this can be compensated for by stronger volcanic outgassing. A weaker $p\text{CO}_2$ weathering dependence (lower β) lengthens the duration of the unfrozen state since the decline in $p\text{CO}_2$ with time has less of an effect on the weathering rate.

To summarize, a temperature-only dependence of the weathering rate ($\beta = 0$) uniquely ties the surface temperature to the volcanic outgassing rate V via Equation (2). A more general dependence on $p\text{CO}_2$ ($\beta > 0$) leads to a richer set of climate solutions, including unstable climate cycles at low enough insolation levels, when weathering equilibrium ceases to exist. These results are not specific to the weathering functional form adopted in Equation (3), in the sense that other weathering laws with a positive dependence on $p\text{CO}_2$ and T_{surf} would lead to qualitatively similar climate behaviors.

4. Conclusions

The key new feature of our analysis is the lack of stable climates on Earth-like planets lacking land vascular plants, at low enough insolation levels (see also Kadoya and Tajika, 2014). This suggests that a subset of Earth-like planets located in the outer regions of habitable zones may be preferentially found in a frozen, rather than deglaciated, state.² A globally frozen state might be observationally inferred from the very high albedo and the correspondingly low water content of the planet's atmosphere. According to these results, some Earth-like planets in the outer habitable zone would also be caught in a transiently warm state with surface liquid water present only infrequently.

The link between unstable climate cycles and the emergence and evolution of life on weakly-insolated Earth-like planets is unclear but possibly important. A reduced amount of time with surface liquid water on planets experiencing climate cycles could in principle slow down the emergence and/or evolution of life (see however Planavsky et al., 2010). On the other hand, life itself could strongly impact the weathering process on weakly-insolated Earth-like planets, as it seems to have done on early Earth (Kump et al., 2000; Schwartzman and Volk, 1989; Berner, 1992, 1994; Berner and Kothavala, 2001; Pierrehumbert, 2010). Although considerable uncertainty remains, the ability of land vascular plants to regulate the soil $p\text{CO}_2$ level that is relevant to the weathering process, well above atmospheric $p\text{CO}_2$ levels, is consistent with these plants effectively decoupling the weathering rate from the atmospheric $p\text{CO}_2$ level (Kump et al., 2000; Schwartzman and Volk, 1989; Berner, 1992, 1994; Berner and Kothavala, 2001; Pierrehumbert, 2010), leading to $\beta \rightarrow 0$ in Equation (3). As a result (Fig. 1, vertical line), the climate of weakly-insolated Earth-like planets could be stabilized against transient cycles once the presence of land vascular plants becomes widespread. This would constitute a strong example of life exerting a feedback on its environment.

Based on these results, one can envision a typical evolutionary path for a habitable planet in orbit around a star that is gradually brightening over time. Repeated snowball events should occur

at earlier times, when insolation is weak and land vascular plants are absent. They should disappear at later times once insolation is strong enough and/or land vascular plants become widespread. In the case of Earth, the Paleoproterozoic and Neoproterozoic snowball events have been interpreted as being caused by an increase in atmospheric O_2 levels and a corresponding decrease in CH_4 levels (Kasting, 2005; Pavlov et al., 2003), rather than the climate cycles highlighted in this work.

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Appendix A. Energy balance climate model

We model the climate of Earth-like planets with a zero-dimensional reduction of a one-dimensional energy balance model (Williams and Kasting, 1997). The model assumes Earth parameters unless otherwise specified (e.g., surface gravity, land/ocean fraction and nitrogen contribution to the total atmospheric mass). Greenhouse effect from atmospheric H_2O and CO_2 are included, with an atmospheric vapor pressure set by surface evaporation (temperature).

The top-of-atmosphere albedo and the outgoing longwave radiation flux are modeled as polynomial fits to a large number of radiative-convective models (Williams and Kasting, 1997). The polynomial fits are functions of surface temperature, partial CO_2 pressure, solar zenith angle and surface albedo. Simple prescriptions for snow/ice coverage, surface albedo and water cloud coverage are adapted from Williams and Kasting (1997). For simplicity, we fix the cosine of the zenith angle to $\mu = 0.4$ and the albedo of ice-free oceans to 0.07 in all the models presented here. We also smooth out the top-of-atmosphere albedo polynomials near the 280 K transition to improve the continuity of the albedo function with temperature.

Based on published results (Kasting et al., 1993), we expect that our results would be quantitatively different, but remain qualitatively valid, for planets that differ modestly from Earth in terms of their surface gravity, land/ocean fraction and/or nitrogen atmospheric content. Note that it has been suggested that weathering does not strongly depend on land/ocean fraction on an Earth-like planet (Abbot et al., 2012). Given the prescriptions adopted, our models are specialized to planets orbiting Sun-like stars. Planets orbiting low-mass M-dwarf stars would experience reduced ice-albedo feedback because of the more reddish nature of the stellar light (Joshi and Haberle, 2012). Preliminary tests indicate that a reduced ice albedo leads to comparatively shorter and lower amplitude climate cycles on such planets.

The energy balance model employed here may not be fully reliable beyond 1.3–1.4 AU, where CO_2 clouds are expected to form and influence the climate (Williams and Kasting, 1997; Selsis et al., 2007). Although the most massive CO_2 atmospheres found in our models only marginally approach hard limits on CO_2 condensation (von Paris et al., 2013), it is also expected that the ice albedo feedback ceases to operate on planets with very massive CO_2 atmospheres ($p\text{CO}_2 > 10$ bars; Wordsworth et al., 2011).

Appendix B. Model simplifications and limitations

Our models are idealized in a number of important ways. In addition to the simplified, zero-dimensional treatment of climate described above, which suggests the possibility of richer behaviors in higher complexity, three-dimensional climate models, our treatment of weathering processes is intentionally simple, in order to

² It is unclear whether such glaciated states would correspond to hard snowballs or milder versions (McKay, 2000; Pollard et al., 2005; Abbot et al., 2011).

isolate the key factors that determine climate stability. We ignore seafloor weathering (Abbot et al., 2012) and the mantle CO₂ cycle (Sleep and Zahnle, 2001).

The absolute calibration of weathering rates in the absence of land vascular plants is unknown, but it is thought to be less than in their presence (Schwartzman and Volk, 1989). For concreteness, we have chosen to calibrate weathering fluxes in our models using current Earth (Bernier, 1994; Bernier and Kothavala, 2001) (Equation (3)). We note that in a model admitting steady-state solutions, a factor three decrease in the weathering rate is equivalent to a factor three increase in the volcanic outgassing rate (see Equation (2)), which is one of the cases shown in Fig. 1 (dotted blue line). Such a model retains the main qualitative feature highlighted in this work, which is the disappearance of stable climate solutions at low enough insolation levels (beyond 1.2 AU for the dotted blue line shown in Fig. 1). Different calibrations in weathering rates and/or volcanic outgassing rates will thus affect our results quantitatively, but our main conclusions should remain valid.

More generally, a planet is likely to change its weathering regime gradually over time, as different forms of life emerge and spread over its surface (Kump et al., 2000; Bernier, 1992). Our models have intentionally focused on the distinction between the absence and presence of land vascular plants, which exemplifies the interplay between life, weathering processes and climate stability.

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